

# D - Alphabetomials

As we all know, there is a big difference between polynomials of degree 4 and those of degree 5. The question of the non-existence of a closed formula for the roots of general degree 5 polynomials produced the famous Galois theory, which, as far as the author sees, bears no relation to our problem here.

We consider only the multi-variable polynomials of degree up to 4, over 26 variables, represented by the set of 26 lowercase English letters. Here is one such polynomial:

$aber + aab + c$

Given a string  $S$ , we evaluate the polynomial on it. The evaluation gives  $p(S)$  as follows: Each variable is substituted with the number of appearances of that letter in  $S$ .

For example, take the polynomial above, and let  $S = \text{"abracadabra edgar"}$ . There are six a's, two b's, one c, one e, and three r's. So

$$p(S) = 6 * 2 * 1 * 3 + 6 * 6 * 2 + 1 = 109.$$

Given a dictionary of distinct words that consist of only lower case letters, we call a string  $S$  a *d*-phrase if

$$S = "S_1 S_2 S_3 \dots S_d",$$

where  $S_i$  is any word in the dictionary, for  $1 \leq i \leq d$ . i.e.,  $S$  is in the form of  $d$  dictionary words separated with spaces. Given a number  $K \leq 10$ , your task is, for each  $1 \leq d \leq K$ , to compute the sum of  $p(S)$  over all the  $d$ -phrases. Since the answers might be big, you are asked to compute the remainder when the answer is divided by 10009.

## Input

The first line contains the number of cases  $T$ .  $T$  test cases follow. The format of each test case is: A line containing an expression  $p$  for the multi-variable polynomial, as described below in this section, then a space, then follows an integer  $K$ . A line with an integer  $n$ , the number of words in the dictionary. Then  $n$  lines, each with a word, consists of only lower case letters. No word will be repeated in the same test case.

We always write a polynomial in the form of a sum of terms; each term is a product of variables. We write  $a^t$  simply as  $t$  a's concatenated together. For example,  $a^2b$  is written as  $aab$ . Variables in each term are always lexicographically non-decreasing.

## Output

For each test case, output a single line in the form

$$\text{Case \#X: sum}_1 \text{ sum}_2 \dots \text{sum}_K$$

where  $X$  is the case number starting from 1, and  $\text{sum}_i$  is the sum of  $p(S)$ , where  $S$  ranges over all  $i$ -phrases, modulo 10009.

## Limits

$$1 \leq T \leq 100.$$

The string  $p$  consists of one or more terms joined by '+'. It will not start nor end with a '+'. There will be at most 5 terms for each  $p$ .

Each term consists at least 1 and at most 4 lower case letters, sorted in non-decreasing order. No two terms in the same polynomial will be the same. Each word is non-empty, consists only of lower case English letters, and will not be longer than 50 characters. No word will be repeated in the same dictionary.

Small dataset

$$1 \leq n \leq 20$$

$$1 \leq K \leq 5$$

Large dataset

$$1 \leq n \leq 100$$

$$1 \leq K \leq 10$$

## Sample

### Input:

```
2
ehw+hwww 5
6
where
when
what
whether
who
whose
a+e+i+o+u 3
4
apple
orange
watermelon
banana
```

### Output:

```
Case #1: 15 1032 7522 6864 253
Case #2: 12 96 576
```