

Lexicographic Order 4

An ordering for the Cartesian product x of any two sets A and B with order relations $<_A$ and $<_B$, respectively, such that if (a_1, b_1) and (a_2, b_2) both belong to $A \times B$, then $(a_1, b_1) < (a_2, b_2)$ iff either

- $a_1 <_A a_2$, or
- $a_1 = a_2$ and $b_1 <_B b_2$.

The lexicographic order can be readily extended to cartesian products of arbitrary length by recursively applying this definition, i.e., by observing that $A \times B \times C = A \times (B \times C)$.

When applied to subsets, two subsets are ordered by their smallest elements. For example, the subsets of $\{1, 2, 3\}$ in lexicographic order are $\{\}, \{1\}, \{1, 2\}, \{1, 2, 3\}, \{1, 3\}, \{2\}, \{2, 3\}, \{3\}$.

You will be given a subset of a set of first n natural numbers. You need to find k -th lexicographically next subset. Also we will consider that lexicographically last subset is followed by the first one in the ordering.

Input

The first line is number t - the amount of test cases. Each test case starts with numbers n and k . The next line describes the given subset. The description starts with number q - the amount of elements in the subset, followed by q natural numbers - the elements of the subset.

Constraints

$1 \leq t \leq 5$
 $1 \leq n \leq 50000$
 $0 \leq k \leq 10000$
 $0 \leq q \leq n$

Output

For each test case output the k -th lexicographically next subset after the given one. If the result is an empty set then print "empty".

Example

Input:

```
3
3 1
1 3
3 3
2 1 3
5 5
0
```

Output:

```
empty
3
1 2 3 4 5
```

