

# Self Numbers

## Background

In 1949 the Indian mathematician D.R. Kaprekar discovered a class of numbers called *self-numbers*. For any positive integer  $n$ , define  $d(n)$  to be  $n$  plus the sum of the digits of  $n$ . (The  $d$  stands for *digitaddition*, a term coined by Kaprekar.) For example:

$$d(75) = 75 + 7 + 5 = 87$$

Given any positive integer  $n$  as a starting point, you can construct the infinite increasing sequence of integers  $n, d(n), d(d(n)), d(d(d(n))), \dots$ . For example, if you start with 33, the next number is  $33 + 3 + 3 = 39$ , the next is  $39 + 3 + 9 = 51$ , the next is  $51 + 5 + 1 = 57$ , and so you generate the sequence

33, 39, 51, 57, 69, 84, 96, 111, 114, 120, 123, 129, 141, ...

The number  $n$  is called a *generator* of  $d(n)$ . In the sequence above, 33 is a generator of 39, 39 is a generator of 51, 51 is a generator of 57, and so on.

Some numbers have more than one generator: For example, 101 has two generators, 91 and 100. A number with no generators is a *self-number*. There are thirteen self-numbers less than 100: 1, 3, 5, 7, 9, 20, 31, 42, 53, 64, 75, 86, and 97.

## Problem

Write a program to output all positive self-numbers less than 1000000 in increasing order, one per line.

## Input

There is no input.

## Output

All positive self-numbers less than 1000000 in increasing order, one per line.